

Could Have

Implies that:

a) something was possible in the past, but is currently not,
"You could have bought it for a cheaper price if you waited."

b) you had the ability to do something in the past, but you chose not to.
"I could have gotten there in time if I had gotten up earlier."

Couldn't Have

Implies that something was not a possibility in the past, even if you wanted it to happen.

"I couldn't have contacted you anyways."

"That couldn't have been him, he was at work at that time."

Can't can also be used interchangeably.

"That can't have been him, he was at work at that time."

Should Have

Implies that something would have been a good idea, but you did not choose to do it.
It can express:

a) a feeling of self-regret,
"I should have accepted the offer."

b) advice about the past,
"You should have kept quiet."

c) what the situation probably would be if everything had gone accordingly, and that it is not certain whether they did or not.
"He should have arrived by now."

Shouldn't Have

Implies that something was not a good idea, but you did it anyways.
"I shouldn't have eaten that much."

Would/Wouldn't Have

a) Can be used as a part of the third conditional with an if clause,

"He would have completed it in time if he wasn't so lazy."

"I wouldn't have even considered it if it wasn't coming from her."

b) Can be used to express that you wanted to or didn't want to do something, but you had to/had not to because of the conditions.

"I would have attended if I wasn't so sick"

"She wouldn't have done it if you didn't insist."

Might/May Have

Implies a guess about something that has happened in the past.

"She might/may have gotten stuck in traffic."

Could can also be used interchangeably.

"She could have gotten stuck in traffic."

Must Have

Implies certainty about something that has happened in the past.

"That must be my dad, he said he would come at eight."